

# 2-6

## Families of Functions



### Vocabulary

#### Review

1. Cross out the item(s) that are NOT *vertical*.

the *y*-axis    the *x*-axis    the horizon    columns    rows

#### Vocabulary Builder

**translation** (noun) trans LAY shun

**Other Word Forms:** translate (verb), translatable (adjective), translation (noun)

**Definition:** A **translation** is a change from one form, state, or appearance to another.

**Math Usage:** A **translation** shifts the graph of a parent function horizontally, vertically, or both without changing its size or shape.

#### Use Your Vocabulary

2. Complete each statement with the correct form of the word *translation*.

NOUN The graph shows a vertical ? of the function.

\_\_\_\_\_

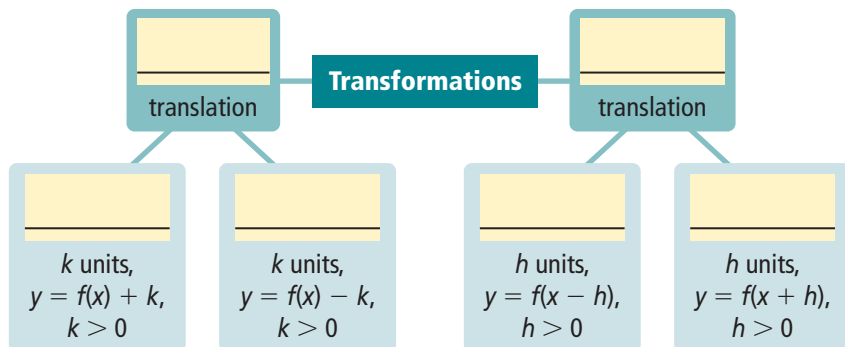
ADJECTIVE The toddler's language was not ?.

\_\_\_\_\_

VERB The Spanish teacher helped the town mayor ? the letter.

\_\_\_\_\_

3. Complete the graphic organizer below.





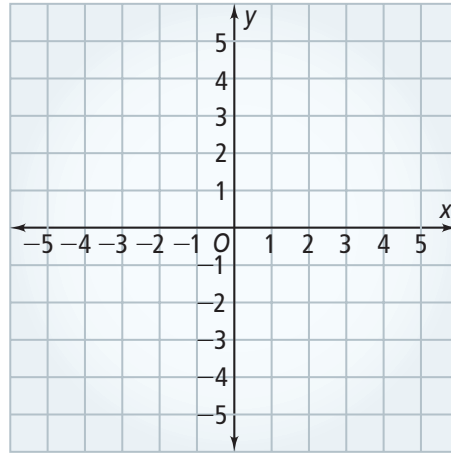
## Problem 1 Vertical Translation

**Got It?** How are the functions  $y = 2x$  and  $y = 2x - 3$  related? How are their graphs related?

4. Complete the table of values.

$x$	$y = 2x$	$y = 2x - 3$
-2	<input type="checkbox"/>	<input type="checkbox"/>
-1	<input type="checkbox"/>	<input type="checkbox"/>
0	<input type="checkbox"/>	<input type="checkbox"/>
1	<input type="checkbox"/>	<input type="checkbox"/>
2	<input type="checkbox"/>	<input type="checkbox"/>

5. Draw the graphs on the coordinate plane below.



6. Write T for *true* or F for *false*.

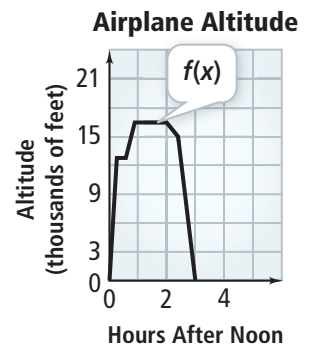
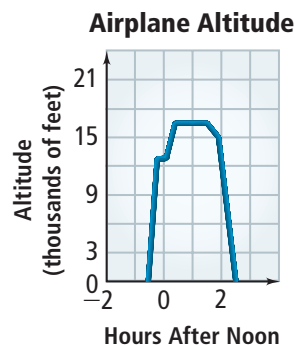
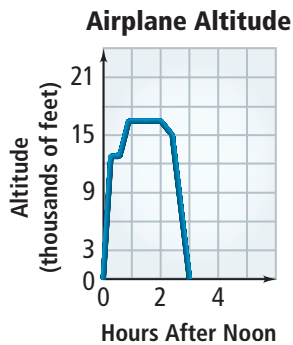
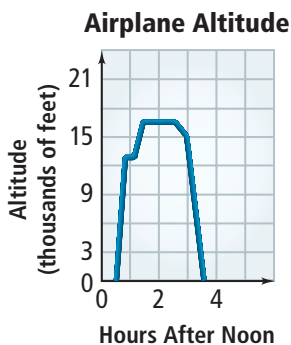
- Each output value for  $y = 2x - 3$  is three less than the corresponding output value for  $y = 2x$ .
- The graph of  $y = 2x - 3$  is the graph of  $y = 2x$  stretched vertically two units.
- The graph of  $y = 2x - 3$  is the graph of  $y = 2x$  translated down three units.
- The graphs of  $y = 2x - 3$  and  $y = 2x$  are parallel.



## Problem 2 Horizontal Translation

**Got It?** The graph shows the projected altitude  $f(x)$  of an airplane scheduled to depart an airport at noon. If the plane leaves 30 minutes early, what function represents this transformation?

7. Circle the graph below that shows the plane leaving 30 minutes early.



8. Circle the function that represents this transformation.

$f(x + 30)$

$f(x - 30)$

$f\left(x + \frac{1}{2}\right)$

$f\left(x - \frac{1}{2}\right)$



### Problem 3 Reflecting a Function Algebraically

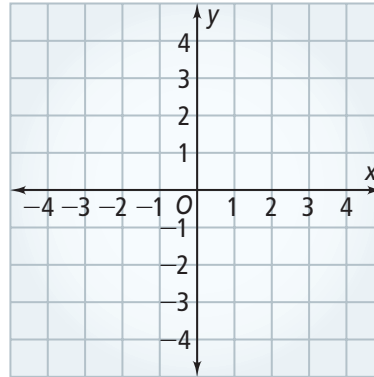
**Got It?** Let  $h(x)$  be the reflection of  $f(x) = 3x + 3$  in the  $x$ -axis. What is a function rule for  $h(x)$ ?

9. Circle the function that shows  $f(x)$  reflected in the  $x$ -axis.

$f(-x)$

$-f(x)$

10. Write the function rule for  $h(x)$  below. Then graph  $h(x)$  and  $f(x)$  to check the reflection.



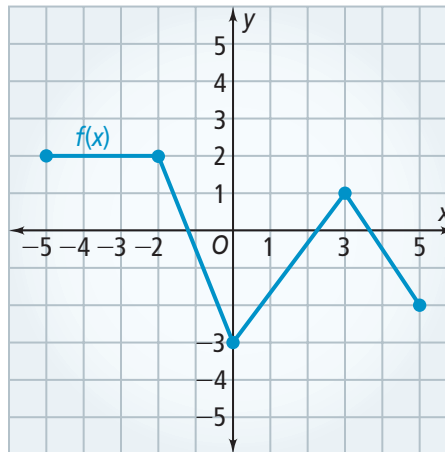
### Problem 4 Stretch and Compression

**Got It?** For the function  $f(x)$  in the table below, what are the corresponding table and graph for the transformation  $h(x) = \frac{1}{3}f(x)$ ?

11. Complete the table of output values.

$x$	$f(x)$	$h(x)$
-5	2	$\frac{2}{3}$
-2	2	
0	-3	
3	1	
5	-2	

12. Graph  $h(x)$  on the coordinate plane below.





## Problem 5 Combining Transformations

**Got It?** The function  $f(x) = x$ . The graph of  $g(x)$  is  $f(x)$  stretched vertically by a factor of 2 and translated down 3 units. What is the function rule for  $g(x)$ ?

13. Underline the correct word or expression to complete each sentence.

The function  $f(x) = x$  stretched vertically by a factor of 2 is

$x + 2$  /  $x - 2$  /  $2x$  /  $-2x$ .

The function  $f(x) = x$  stretched vertically by a factor of 2 and then translated down 3 units is

$-2x + 3$  /  $2x - 3$  /  $-2x - 3$  /  $2x + 3$ .

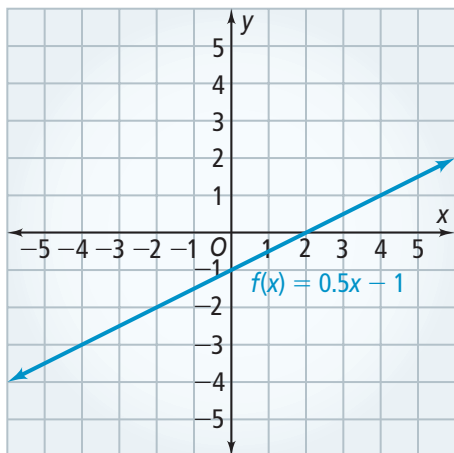
14. The function rule for the combined transformation is



## Lesson Check • Do you UNDERSTAND?

**Compare and Contrast** The graph below shows  $f(x) = 0.5x - 1$ . Graph  $g(x)$  by translating  $f(x)$  up 2 units and then stretching it vertically by a factor of 2. Graph  $h(x)$  by stretching  $f(x)$  by a factor of 2 and then translating it up 2 units. Compare the graphs of  $g(x)$  and  $h(x)$ .

15. Graph  $g(x)$  and  $h(x)$ .



16. Underline the correct word(s) or expression to complete each sentence or equation.

$g(x)$  and  $h(x)$  are / are not the same function.

$g(x) = x + 2$  /  $x - 2$  /  $x$  /  $-x$

$h(x) = x + 2$  /  $x - 2$  /  $x$  /  $-x$

$g(x)$  and  $h(x)$  are

the same / parallel / perpendicular lines.



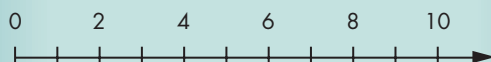
## Math Success

Check off the vocabulary words that you understand.

translation    reflection    transformation    stretch    compression

Rate how well you can *transform linear functions*.

Need to review



Now I get it!